

*Note:* The KSM03 development of the Earth TGP transformed into HW95 normalization and format is available in file <http://www.eas.slu.edu/GGP/kudryavtsev/ksm03.dat>

## Description of Data Available in File **tgp\_coefficients.dat** (original KSM03 format)

The data are a series of harmonic coefficients  $C_{nm}$ ,  $S_{nm}$  of the Earth tide generating potential (TGP) expansion, named KSM03

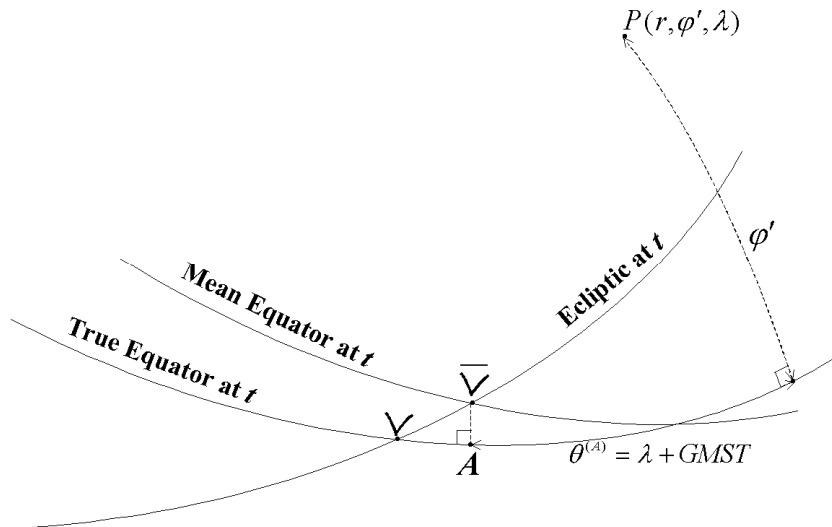
$$V(t) = \sum_{n=2}^{\infty} \sum_{m=0}^n \left( \frac{r}{R_E} \right)^n \bar{P}_{nm}(\sin \varphi') [C_{nm}(t) \cos m\theta^{(A)}(t) + S_{nm}(t) \sin m\theta^{(A)}(t)] + \frac{r}{R_E} \left\{ \bar{P}_{10}(\sin \varphi') C_{10}(t) + \bar{P}_{11}(\sin \varphi') [C_{11}(t) \cos \theta^{(A)}(t) + S_{11}(t) \sin \theta^{(A)}(t)] \right\}. \quad (1)$$

where  $V$  is the value of the TGP at an arbitrary point  $P$  on Earth's surface at epoch  $t$ ,  $R_E$  is the mean Earth equatorial radius (=6378136.3 m),  $r$  is the geocentric distance to  $P$ ,  $\varphi'$  is the geocentric latitude of  $P$ ,  $\theta^{(A)}(t)$  is the local sidereal time at  $P$  reckoned along the true geoequator of date from the origin point  $A$  - that being the projection of the mean equinox of date (see Fig.1) - so that  $\theta^{(A)}(t)$  is related to the Earth fixed east longitude (from Greenwich)  $\lambda$  as

$$\theta^{(A)}(t) = \lambda + GMST \quad (2)$$

( $GMST$  is Greenwich Mean Sidereal Time defined by a well-known expression by Aoki et al. 1982, *Astron. Astrophys.* 105: 359-361);  $\bar{P}_{nm}$  is the normalized associated Legendre function related to the unnormalized one ( $P_{nm}$ ) as

$$\bar{P}_{nm} = N_{nm} P_{nm} \quad \text{where } N_{nm} = \sqrt{\frac{\delta_m (2n+1)(n-m)!}{(n+m)!}} \quad \text{and } \delta_m = \begin{cases} 1 & \text{if } m = 0 \\ 2 & \text{if } m \neq 0. \end{cases} \quad (3)$$



**Figure 1.** The reference frame used in KSM03 development of the Earth TGP

Every coefficient  $C_{nm}$ ,  $S_{nm}$  is represented by a Poisson series like

$$C(S)_{nm}(t) = \sum_{k=1}^N \left\{ [A_{k0}^c + A_{k1}^c t + A_{k2}^c t^2] \cos \omega_k(t) + [A_{k0}^s + A_{k1}^s t + A_{k2}^s t^2] \sin \omega_k(t) \right\} \quad (4)$$

where  $A_{k0}^c, A_{k1}^c, \dots, A_{k2}^s$  are constants and  $\omega_k(t)$  are 4<sup>th</sup>-degree polynomials of time

$$\omega_k(t) = \nu_k t + \nu_{k2} t^2 + \nu_{k3} t^3 + \nu_{k4} t^4. \quad (5)$$

The file **tgp\_coefficients.dat** includes the following data (notations are defined in (1)-(5))

Line 1:  $N$  (non-dimensional; format I12)

Lines 2, 9, 16, ..., 187266: blank

Lines 3, 10, 17, ..., 187267:  $k$  (non-dimensional; format I12)

Lines 4, 11, 18, ..., 187268: notation of a coefficient ( $C$  or  $S$ ) to which the expansion term relates;  $n$ ;  $m$ ; multipliers of six major planets' mean longitudes (Mercury – Saturn), of mean longitude of the lunar ascending node  $\Omega$ , and of Delaunay variables  $D, l', l, F$  used to calculate the 4th-order frequency  $\omega_k(t)$  of the expansion term (all non-dimensional; format 1X,A,1X,2I3,1X,1I3)

Lines 5, 12, 19, ..., 187269:  $\sqrt{A_{k0}^c{}^2 + A_{k0}^s{}^2}, \sqrt{A_{k1}^c{}^2 + A_{k1}^s{}^2}, \sqrt{A_{k2}^c{}^2 + A_{k2}^s{}^2}$   
(dimension  $\text{m}^2/\text{sec}^2, \text{m}^2/\text{sec}^2/\text{day}, \text{m}^2/\text{sec}^2/\text{day}^2$ , respectively; format 3D24.15)

Lines 6, 13, 20, ..., 187270:  $A_{k0}^c, A_{k1}^c, A_{k2}^c$  (dimension  $\text{m}^2/\text{sec}^2, \text{m}^2/\text{sec}^2/\text{day}, \text{m}^2/\text{sec}^2/\text{day}^2$ , respectively; format 3D24.15)

Lines 7, 14, 21, ..., 187271:  $A_{k0}^s, A_{k1}^s, A_{k2}^s$  (dimension  $\text{m}^2/\text{sec}^2, \text{m}^2/\text{sec}^2/\text{day}, \text{m}^2/\text{sec}^2/\text{day}^2$ , respectively; format 3D24.15)

Lines 8, 15, 22, ..., 187272:  $\nu_k, \nu_{k2}, \nu_{k3}, \nu_{k4}$  (dimension  $\text{rad}/\text{day}, \text{rad}/\text{day}^2, \text{rad}/\text{day}^3, \text{rad}/\text{day}^4$ , respectively; format 4D24.15)

The time  $t$  (TDT) has to be counted in Julian days from epoch J2000.0 (JED 2451545).

Details can be found in Kudryavtsev S.M. «Improved Harmonic Development of the Earth Tide Generating Potential», *Journal of Geodesy*, 2004, vol. 77, N 12, pp. 829-838